Minimal Representation for the Control of the Adept Quattro with Rigid Platform via Leg Observation Considering a Hidden Robot Model

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Abstract—Previous works on the Gough-Stewart (GS) platform have shown that its visual servoing using the observation of its leg directions was possible by observing only three of its six legs but that the convergence to the desired pose was not guaranteed. This can be explained by considering that the visual servoing of the leg direction of the GS platform was equivalent to controlling another robot, the 3-UPS that has assembly modes and singular configurations different from those of the GS platform. Considering this hidden robot model allowed the simplification of the singularity analysis of the mapping between the leg direction space and the Cartesian space.

In this paper, the work on the definition of the hidden robot models involved in the visual servoing using the observation of the robot leg directions is extended to another robot, the Adept Quattro. It will be shown that the hidden robot model is completely different from the model involved in the control of the GS platform. Therefore, the results obtained for the GS platform are not valuable for this robot. The hidden robot has assembly modes and singular configurations different from those of the Quattro. An accuracy analysis is performed to show the importance of the leg selection. All these results are validated on a Quattro simulator created using ADAMS/Controls and interfaced with Matlab/Simulink.

I. INTRODUCTION

Compared to serial robots, parallel robots are stiffer and can reach higher speeds and accelerations [1]. However, their control is more complex because of the highly coupled mechanical structure and many other factors (e.g. clearances, assembly errors, etc.) which degrade stability and accuracy.

Many research papers focus on the control of parallel mechanisms (see [2] for a long list of references). Cartesian control is naturally achieved through the use of the inverse differential kinematic model which transforms Cartesian velocities into joint velocities. It is noticeable that, in a general manner, the inverse differential kinematic model of parallel mechanisms does not only depend on the joint configuration (as for serial mechanisms) but also on the end-effector pose. Consequently, one needs to be able to estimate or measure the latter.

Past research works have proved that the robot end-effector pose can be effectively estimated by vision. The most common approach consists of the direct observation of the end-effector pose [3], [4], [5]. However, some applications prevent the observation of the end-effector of a parallel mechanism by vision. For instance, it is not wise to imagine observing the end-effector of a machine-tool while it is generally not a problem to observe its legs that are most often designed with slim and rectilinear rods [2].

A first step in this direction was made in [6] where vision was used to derive a visual servoing scheme based on the observation of a Gough-Stewart (GS) parallel robot [7]. In that method, the leg directions were chosen as visual primitives and control was derived based on their reconstruction from the image. In this work, it has also been observed that:

1) the GS platform can be controlled using the observation of only three leg directions (arbitrarily chosen among its six legs), and that

2) in some cases, the GS platform does not converge to the desired end-effector pose (even if the observed leg directions did)

without finding some concrete explanations to these points.

Recently, two of the authors of the present paper have demonstrated in [8] that these two points could be explained by considering that the visual servoing of the leg direction of the GS platform was equivalent to controlling another robot, the 3-UPS (where \( U \) stands for an actuated universal joint, \( P \) and \( S \) for passive prismatic and spherical joints, respectively) that has assembly modes and singular configurations different from those of the GS platform. Considering this hidden robot model allowed the simplification of the singularity analysis of the mapping between the leg direction space and the Cartesian space by reducing the problem to the singularity analysis of a new robot and it was possible to find simple geometric conditions for the singular configurations.

In this paper, the visual servoing of the Adept Quattro using leg observation is considered. It will be shown that another hidden robot model (with a kinematic chain completely different from the 3-UPS, i.e. the hidden model for the vision based control of the GS platform) is involved in this kind of control. Consequently, the assembly modes and singularity conditions of this hidden robot are totally different from those of the 3-UPS and the results obtained in [8] are not valuable for the Quattro.

II. CONTROL OF THE ADEPT QUATTRO WITH RIGID PLATFORM USING LEG OBSERVATION

This part aims at presenting the servoing of the Adept Quattro robot with rigid platform using leg observation.
A. Kinematics of the Quattro with rigid platform

The Quattro (Fig. 1) is composed of four identical kinematic chains (legs), that carry the articulated moving platform. Each of the 4 kinematic chains is actuated from the base by a rotary motor, located at point $A_i$. This motor rotates a proximal link that is linked to an articulated parallelogram, itself attached to the moving platform. The parallelogram consists of two slim and cylindrical shaped rods fitted with ball-joints at points $B_{i1}, B_{i2}, C_{i1}$ and $C_{i2}$. As a result, each kinematic chain is a $R(2–SS)$ leg (where $R$ stands for an actuated revolute joint).

There exist two versions of the Quattro: one with a rigid (non-articulated) moving platform, thus leading to a redundant parallel robot with 3 translational degrees of freedom (dof) of the end-effector, and the other with an articulated platform that allows a supplementary rotation of the end-effector around the vertical axis $z$. This paper focuses only on the Quattro with the rigid platform, i.e. with 3 translational dof.

In the following of the paper, the notations detailed below are used:

- point $B_i$ ($C_i$, resp.) is at the middle of segment $B_{i1}B_{i2}$ ($C_{i1}C_{i2}$, resp.) (Fig 1(b)),
- point $P$, the controlled point of the platform, is the barycentre of points $C_i$; its coordinates are denoted as $P$ and its velocity as $\dot{P}$,
- $A_j (B_i, C_i, \text{resp.})$ is the vector of coordinates of point $A_j (B_i, C_i, \text{resp.})$,
- $q_i$ is the angular coordinate of the actuator $i$, and is defined as the angle between the axis $x_i$ (the projection of vector $A_iB_i$ in the horizontal plane $(Oxy)$) and $\overline{AB_i}$ (Fig. 1(b)),
- $l_1$ is the length of the proximal link, and $l_2$ the length of one rod of the parallelogram.

Moreover, the superscript ‘$i$’ will be used before the vectors to indicate that the vector coordinates are expressed in the leg local frame $(Ox_i,y_i,z_i)$. If no superscript is used, the vector is expressed in the base frame.

The usual inverse kinematics of the Quattro with rigid platform can be computed using the following loop-closure equations (Fig. 1):

$$^{i}C_i - ^iB_i = l_2^i \mathbf{u}_i$$  \hspace{1cm} (1)

where

$$^{i}B_i = ^iA_i + l_1 [\cos q_i \hspace{0.5cm} 0 \hspace{0.5cm} \sin q_i]^T = ^iA_i + l_1^i \mathbf{v}_i$$  \hspace{1cm} (2)

Squaring both sides of (1) and introducing (2) leads to

$$(x_{A,C_i} - l_1 \cos q_i)^2 + y_{A,C_i}^2 + (z_{A,C_i} - l_1 \sin q_i)^2 - l_2^2 = 0$$  \hspace{1cm} (3)

where $^{i}C_i - ^iA_i = [x_{A,C_i}, y_{A,C_i}, z_{A,C_i}]^T$. (3) can be finally solved as a second order polynomial in $\tan(q_i/2)$ by replacing $\cos q_i$ by $\left(1 - t_i^2\right)/\left(1 + t_i^2\right)$ and $\sin q_i$ by $2t_i/\left(1 + t_i^2\right)$, where $t_i = \tan(q_i/2)$. Skipping all mathematical derivations, it comes that:

$$q_i = 2 \tan^{-1} \left( \frac{-\beta_i \pm \sqrt{\beta_i^2 + \beta_i^2 - \gamma_i^2}}{\gamma_i - \alpha_i} \right)$$  \hspace{1cm} (4)

The first-order kinematics that relates the platform translational velocity $\dot{\tau}_p$ to the actuator velocities can be obtained through the differentiation of (3) with respect to time and can be expressed as:

$$\mathbf{A}_p \dot{\tau}_p + \mathbf{B} q = 0$$  \hspace{1cm} (6)

where the $i$-th line of $\mathbf{A}$ can be written as

$$a_i = l_2^i \mathbf{u}_i^T$$  \hspace{1cm} (7)

and $\mathbf{B}$ is a diagonal matrix whose $i$-th diagonal term is

$$b_i = l_1^i l_2^i \mathbf{u}_i^T \mathbf{Y}_i^T, \quad \mathbf{Y}_i^T = \begin{bmatrix} -\sin q_i & 0 & \cos q_i \end{bmatrix}^T$$  \hspace{1cm} (8)

It should be mentioned that $\mathbf{A}$ is a $4 \times 3$ rectangular matrix. As a result,

$$\dot{q} = -\mathbf{B}^{-1} \mathbf{A} \tau_p = \mathbf{J}_{inv} \tau_p$$, or also $\tau_p = \mathbf{J}_{inv}^+ \dot{q}$  \hspace{1cm} (9)

where $\mathbf{J}_{inv}$ is the pseudo-inverse of $\mathbf{J}_{inv}$.

B. Kinematics of the Quattro using leg observation

The servoing of the Adept Quattro robot with rigid platform using leg observation proposes to observe the parallelogram direction $\mathbf{u}_i$ to control the robot displacements. $\mathbf{u}_i$ can be obtained directly from (1)

$$\mathbf{u}_i = (C_i - B_i) / l_2$$  \hspace{1cm} (10)

Introducing (2) into (10) and differentiating (10) with respect to time leads to:

$$\dot{\mathbf{u}}_i = (\tau_p - l_1^i \mathbf{Y}_i^T \dot{q}_i) / l_2$$  \hspace{1cm} (11)

Finally, from (9), it comes that:

$$\dot{\mathbf{u}}_i = (\mathbf{I}_3 + l_1^i \mathbf{Y}_i^T \mathbf{a}_i/b_i) / l_2 \tau_p = \mathbf{M}_i^T \tau_p$$  \hspace{1cm} (12)

where $\mathbf{I}_3$ is the $3 \times 3$ identity matrix and matrix $\mathbf{M}_i^T$ is called the interaction matrix.

It can be proved that matrix $\mathbf{M}_i^T$ is of rank 2 [6]. As a result, a minimum of two independent legs is necessary to control the end-effector pose. An interaction matrix $\mathbf{M}_i^T$ can then be obtained by stacking the matrices $\mathbf{M}_i^T$ of $k$ legs ($k = 2...4$).
Then, introducing the placement of the leg directions \( u_i \) where \( c_k \) legs (the antisymmetric matrix associated to a 3D vector \([5]\)), the standard vector difference. Consequently, the error grounding the proposed control law will be:

\[
E_i = \lambda c_k e(s, s_d) \tag{14}
\]

where \( T_c \) is used as a pseudo-control variable and the superscript \(+\) corresponds to the matrix pseudo-inverse.

The visual primitives being unit vectors, it is theoretically more elegant to use the geodesic error rather than the standard vector difference. Consequently, the error grounding the proposed control law will be:

\[
e_i = u_i \times \frac{d}{dt}u_i \tag{15}
\]

Finally, a control is chosen such that \( E \), the vector stacking the errors \( e_i \) associated to \( k \) legs (\( k = 2...4 \)), decreases exponentially, i.e. such that

\[
\dot{E} = -\lambda E \tag{16}
\]

Then, introducing \( N_T^T = -[u_i] \times M_T^T \) (where \([-] \times \) is the antisymmetric matrix associated to a 3D vector \([5]\)), the combination of (12), (15) and (16) gives

\[
\tau_p = -\lambda N_T^T + E \tag{17}
\]

where \( N_T \) can be obtained by stacking the matrices \( N_T^T \) of \( k \) legs (\( k = 2...4 \)).

This expression can be transformed into the control joint velocities using (9):

\[
\dot{q} = -\lambda J_{steq} N_T^T + E \tag{18}
\]

In the next section, it is shown that observing the displacement of the leg directions \( u_i \) is intrinsically equivalent to controlling another robot, different from the Quattro.

**III. DESCRIPTION OF THE HIDDEN ROBOT MODEL**

**A. Description of the hidden robot architecture**

In [8], it has been demonstrated that the visual servoing of the leg directions of the GS platform was equivalent to controlling another virtual robot composed of \( UPS \) legs, for which the measure of the vectors \( u_i \) was an image of the displacements of the actuated \( U \) joints. So, in a reciprocal manner, one could wonder what kind of virtual equivalent leg is involved in the visual servoing of the Quattro using leg directions.

The virtual equivalent leg for the Quattro must:
- guaranty that the kinematic relations (4), (9), (10) and (12) are still valid,
- ensure that, when only two legs are observed, the equivalent robot made of the two virtual legs is able to keep the platform orientation constant,
- contain active \( U \) joints that can be related to the measure of \( u_i \), i.e. these joints should move if and only if the value of \( u_i \) is changing.

Considering these three points, it could be proved by a simple kinematic analysis that the equivalent leg has a II(2–\( U \)) architecture, (where II stands for a planar parallelogram linkage joint – Fig. 2(a)). The II joint keeps constant the orientation of the rod \( B_3 \rightarrow B_4 \) (Fig. 2(b)) and garanties that, as long as the vector \( u_i \) is set at a constant value, the first \( U \) joints (that link the planar and spatial parallelograms) are not moving. The passive \( U \) joints linked to the platform prevent its rotation when only two legs are used. Thus, observing the direction of the Quattro leg remains not to control the displacement of a II(2–SS) leg but of a virtual II(2–\( U \)) leg with the same geometric properties as the real leg (\(|A_1 B_i| = l_1, |B_i C_i| = l_2\) in Fig. 2).

It can be demonstrated that a II(2–\( U \)) robot (Fig. 3(a)) is fully-actuated. Therefore, this is the reason why it is possible to control the Quattro by observing the displacements of two of its four legs. This is equivalent to actuate a virtual II(2–\( U \)) robot with the same geometric properties as the Quattro (same attachment points, leg length, etc.), but with assembly modes and singular configurations that differ from those of the Quattro. They should be studied in order to avoid control problems.
B. Forward kinematic analysis

Using the developed form of (1) and (2), it comes that:

\[
\begin{bmatrix}
  x_{A,C_i} - l_2 u_i^x \\
y_{A,C_i} - l_2 u_i^y \\
z_{A,C_i} - l_2 u_i^z 
\end{bmatrix}
= l_1 \begin{bmatrix}
  \cos q_i \\
  0 \\
  \sin q_i
\end{bmatrix}
\]  
(19)

where \( u_i^T = [u_i^x, u_i^y, u_i^z]^T \). Rearranging the terms of (19) and developing the expressions, a set of equations can be obtained (for \( i = 1 \cdots 4 \))

\[
l_1^2 = (\chi x - x_{S_i})^2 + (\chi z - z_{S_i})^2 - (\gamma y - y_{S_i})
\]  
(20)

where \( \chi S_i = [x_{S_i}, y_{S_i}, z_{S_i}]^T = \chi A_i + l_2 \chi u_i + \chi C_i \chi P \) and \( \chi P = [\chi x, \chi y, \chi z]^T \). Equations (20) are equations of circles, denoted as \( \mathcal{L}_i \), of radius \( l_1 \), located in planes \( y = y_{S_i} \), and centred in point \( S_i \), of coordinates \( \chi S_i \). These circles represent the vertex space of the tip of the leg \( i \), when the vector \( \chi u_i \) is fixed and the planar parallelogram passively moving (Fig. 2(b)) [1]. As a result, the forward kinematic problem \( (\beta p) \) is equivalent to finding the intersection between the circles \( \mathcal{L}_i \) of the observed legs. In conclusion, it may exist 0, 1 unique solution, 1 double solution (singularity condition), 2 distinct solutions or infinite number of solutions (if the circles are superposed, which is also a singularity condition) to the \( \beta p \).

Thus, the 2–II(2–U) robot can have up to two distinct assembly modes that are different from those of the Quattro. The existence of these assembly modes explains the second point presented in the introduction, i.e. the non systematic convergence of the end-effector of the observed robots to the desired pose, even if the observed leg directions do. A numerical example of this phenomenon will be presented in the section V.

C. Singularity analysis

Three types of singular configurations, related to the degeneracy of the first-order kinematics, may appear for robots [10]:
1) the Type 1 singularities where the robot loses at least one degree of freedom;
2) the Type 2 singularities where there is the apparition of some uncontrollable motions. In their neighborhood, the platform accuracy considerably decreases;
3) the Type 3 singularities, where both Type 1 and Type 2 singularities encounter.

There exist other types of singularities, such as the constraint singularities [11], but they are due to passive constraint degeneracy only, and are not involved in the mapping between the leg directions and the Quattro end-effector space.

For the 2–II(2–U) robot, Type 1 singularities appear when \( A_i B_i \) and \( B_i C_i \) are colinear. In such cases, the robot reaches its workspace boundary. Type 2 singularities appear when the planes \( P_i \) and \( P_j \) (whose normal vectors are equal to \( \chi v_i^+ \) and \( \chi v_j^+ \), resp.) are parallel. In such cases, the circles \( \mathcal{L}_i \) and \( \mathcal{L}_j \) have a common tangent at their intersection point and the robot gains one uncontrollable \( \text{dof} \) along this tangent (Fig. 3(b)).

Obviously, the singularity loci vary depending on the leg chosen for the Quattro control. Therefore, it is extremely important, for having the best performances of the controller, to make an optimal selection of the legs to observe. This is the topic of the next section.

Finally, it should be mentioned that the singularities of the 2–II(2–U) robot are not physical singularities, in the sense that they do not lead to uncontrollable free motions of the platform. However, they are representation singularities due to the mapping from the Cartesian space to the leg direction space [12].

IV. SELECTION OF THE CONTROLLED LEGS

Several indices can be used for characterizing the neighborhood of singularities (e.g. the condition number, the dexterity [13], etc.). Here, as generally, the visual servoing is used for improving the robot accuracy, it is proposed to use it as an index for the characterization of singularity proximity.

A. Accuracy analysis

From (12), and using the first order approximation of the forward geometric model [13], it is possible to write

\[
\delta \mathbf{p} = \mathbf{M}^T + \delta \mathbf{u}
\]  
(21)

where \( \delta \mathbf{p} \) is the platform positioning error, \( \delta \mathbf{u} \) is the error on the observation of the leg direction, and \( \mathbf{M}^T + \) is the pseudo-inverse of the matrix \( \mathbf{M}^T \) that can be obtained by stacking the matrices \( \mathbf{M}_i^T \) of the observed legs. Obviously, this matrix is the Jacobian matrix of the equivalent 2–II(2–U) robot and, as a result, will degenerate near the singularity configurations presented in section III-C. It should be mentioned here that it is decided to use a simple model for computing the robot accuracy, but any other more complicated models can be used (e.g. models that take into account flexibilities [14], clearances [15], etc.). However, this simple model is enough for our demonstration.

The Adept Quattro has the following characteristics:
1) \( l_1 = 0.380 \text{m}, l_2 = 0.825 \text{m} \),
2) \( A_i = 0.296 \cos \theta_i, \sin \theta_i, 0 \)^T (in meters)
3) \( PC_i = 0.102 \cos \theta_i, \sin \theta_i, 0 \)^T (in meters)
4) \( \theta_i = [-3 \pi/4, -\pi/4, \pi/4, 3\pi/4] \) (in radians)

For this mechanism, and for an error \( \delta \mathbf{u} \), defined such that the vector \( \mathbf{u}_i \) is contained in a cone of axis \( \mathbf{u}_{10} \) and of half angle \( \phi_i \) (\( \mathbf{u}_{10} \) is the nominal value of \( \mathbf{u}_i \)), and in what follows, \( \phi_i \) is taken equal to 0.01 deg. for each leg direction), let us compute the maximal positioning error when only two of its four legs are observed. Six different combinations are possible. However, the value of the error for only two of them (when legs \{1,2\} and \{1,3\} are observed) is plotted at Fig. 4.

On Fig. 4(a), it is possible to note that the maximal error varies very quickly, especially near singularity. On Fig. 4(b), things are different. The variation of the accuracy is very smooth. Thus, it can be concluded that the selection of the legs to observe is crucial for the final pose accuracy.
B. Discussion

The previous section showed the importance of the legs chosen for the control scheme. Several questions naturally arise here. The first one concerns the number of legs to observe. In terms of accuracy, it is obvious that observing three or four legs, i.e. adding measurement redundancy, will improve the pose accuracy of the robot. However, increasing the number of legs to observe leads to an increase of the computational time for any given application.

The second question is about the selection of the legs to observe. With only two legs among four to observe, as mentioned above, six different $2-II(2–UU)$ robots can be defined. What is thus the best virtual robot model to use?

If the control law proposed in section II-C is applied, it is first necessary to guaranty that, for the used set of legs: 

- the initial and final robot configurations must be included in the same assembly mode of the virtual $2-II(2–UU)$ robot. If not, the controller will not be able to converge to the desired end-effector pose, even if the observed leg directions do. In this last case, the problem can be solved by applying special trajectories that cross Type 2 singularities \cite{16} or encircle a cusp point \cite{17}.

Then, if accuracy is needed, the leg selection must guaranty the best final accuracy. To achieve this goal, the following procedure can be used:

1) knowing the four leg orientations at the initial and final Quattro configurations, compute the solutions of the $fkp$ of the six $2-II(2–UU)$ robots,

2) find, using a procedure similar to the one proposed in \cite{18} for all virtual $2-II(2–UU)$ robots, the solutions of the $fkp$ that belong to the same assembly mode; if, for one given virtual robot, initial and final platform configurations do not belong to the same assembly mode, discard it; if it does not exist any $2-II(2–UU)$ robot for which initial and final configurations belong to the same assembly mode, the displacement is not feasible, except if special trajectories are planned as mentioned previously,

3) for all remaining virtual $2-II(2–UU)$ robots, knowing the observation error $\delta_{\text{U}}$, compute the positioning error using (21); retain the set of legs that guaranty the best accuracy;

4) test the controller (in simulation) with the retained set of legs; if there is no problem of convergence and that the legs are observable during the whole displacement, the problem is solved; if not, discard this set of leg and redo point 3; if it does not exist any $2-II(2–UU)$ robot for which initial and final configurations belong to the same assembly mode, the displacement is not feasible, except with special trajectories.

Obviously, this methodology can be extended when three or four legs are observed. One should also be aware that instead of given the initial and final robot configurations to the controller, it is better to define a trajectory between these two points in order to avoid crossing singularities inadvertently.

Finally, it is considered in this paper that the sensor measurement space is the same as the leg direction space. However, for example using a camera, the leg directions are not directly measured but rebuilt from the observation of the legs limbs projection in the 2D camera space \cite{6}. Thus, for the leg reconstruction, the mapping between the camera space and the real 3D space is involved, and it is not free of singularities (see \cite{19} for an example of mapping singularities). In the neighborhood of mapping singularities, the robot accuracy will also tend to decrease. As a result, this mapping should be considered in the accuracy computation and in the selection of the legs to observe.

V. SIMULATION RESULTS

In this section, simulations are performed on an ADAMS mockup of the Adept Quattro. This virtual mockup is connected to Matlab/Simulink via the module ADAMS/Controls. The controller presented in section II-C is applied (with $\lambda \approx 5$).

In the first simulations, the initial platform pose is equal to $\{x = 0.1m, y = 0.04m, z = -0.93m\}$ and the final platform pose is set to $\{x = 0m, y = -0.25m, z = -0.7m\}$. For going from the initial point to the final ones, two sets of observed leg directions are tested: $\{1, 2\}$ and $\{1, 3\}$. The results for the convergence of the leg directions are presented in Fig. 5. It can be shown that when the legs $\{1, 3\}$ are observed, all leg directions converge to 0. This is not true for the second case. Looking at the platform pose computed by ADAMS, the robot reach the configuration $\{x = 0m, y = -0.25m, z = -0.958(m)\}$ (Fig 6). Solving the forward geometric problem using (20) at the final desired robot configuration for legs $\{1, 2\}$, it can be demonstrated that two real assembly modes exist that are $\{x = 0m, y = -0.25m, z = -0.7m\}$ and $\{x = 0m, y = -0.25m, z = -0.958m\}$. This validates the theory presented in section III.

In the second simulation, the final point is changed to $\{x = 0m, y = -0.3m, z = -0.85m\}$ and a random noise of 0.01 deg. is added on the simulated measure of the leg directions. To show the importance of the leg selection on the
robot accuracy, it is decided to control the robot displacement using three different sets of legs: (i) legs \{1, 2\}, (ii) legs \{1, 3\} and (iii) all legs. The results (Fig. 7(a)) show that, as presented in Fig. 4, the final platform pose accuracy is better when legs \{1, 3\} are observed (around 0.22mm) than with legs \{1, 2\} (around 1.6mm). When all legs are observed, the final pose error is a bit lower lower than when only two legs are observed (0.15mm). This seems normal. However, it can be proved that observing the four legs does not lead to a mapping without any singularities. A singular configuration still exists when all the planes \(P_i\) for the four legs are horizontal, which can be difficult to detect without studying the equivalent robot model. Finally, for testing the robustness of the controller, the noise is multiplied by 10, but we can still observe a convergence of the platform to the desired pose (Fig. 7(b)).

VI. CONCLUSIONS

This paper presented new insights about the sensor-based control of the Adept Quattro. It has been shown that observing the leg directions of the Quattro involves controlling the displacement of a hidden robot which is based on \(\Pi(2–UU)\) legs instead of \(R(2–SS)\) legs. If only two legs are observed, the new equivalent robot becomes a \(2–\Pi(2–UU)\) robot that has up to two distinct assembly modes that are different from those of the Quattro. Its conditions of singularities have been presented. It has been shown that the legs to observe should be chosen carefully in order to avoid inaccuracy problems.

All the presented results have been validated on a Quattro simulator created using ADAMS/Controls and interfaced with Matlab/Simulink. Future works will concern the generalization of the concept of hidden robot model for different classes of parallel robots and the experimental validations.

REFERENCES