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# Outline

- 1 Introduction
- 2 The model
- 3 Testing IOPOAs
- 4 Other testing questions
- 5 Further Research

# General problem

## The specification

- We consider that a formal specification of the system is provided
- The specification is given via an automata
- We are provided with an implementation of the specification, which may or may not be correct

# General problem

## The test

- The implementation is a black box with which we can interact
- We want to automatically generate test sequences to prove properties such as:
  - The conformance of the implementation to the specification
  - Homing and synchronizing sequences
  - State identification and State Verification

# Sequential Systems

## Definition

A deterministic FSM  $M$  is defined by a tuple  $(S, s_1, X, Y, \delta, \lambda)$

- $S$  is a finite set of *states*
- $s_1 \in S$  is the *initial state*
- $X$  is the finite *input alphabet*
- $Y$  is the finite *output alphabet*
- $\delta : S \times X \rightarrow S$  is the *next state function*
- $\lambda : S \times X \rightarrow Y$  is the *output function*

In the following, we assume that our FSMs are deterministic, complete and minimized.

# Sequential Systems

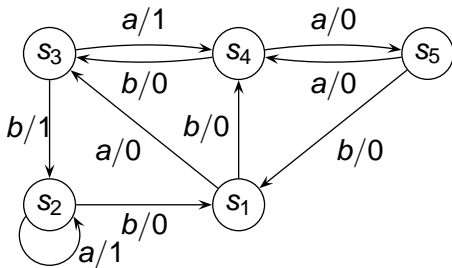


Figure: The FSM  $M_0$

In  $M_0$

- $S = \{s_1, s_2, s_3, s_4, s_5\}$
- $X = \{a, b\}$
- $Y = \{0, 1\}$

# Concurrent multi-port machines

## Definition

A  **$p$ -multiport deterministic FSM**  $M$  is defined by a tuple  $(S, s_1, p, X_1, X_2, \dots, X_p, \delta, Y_1, Y_2, \dots, Y_p, \lambda_1, \lambda_2, \dots, \lambda_p)$

- $S$  is a finite set of  $n$  states
- $s_1 \in S$  is the *initial state*
- $X_i$  is the set of input symbols on port  $i$  such that for  $j \in [1 \dots p]$  and  $j \neq i$ ,  $X_i \cap X_j = \emptyset$ .
- $Y_i$  is the set of output symbols on port  $i$  such that for  $i, j \in [p]$  if  $i \neq j$  then  $Y_i \cap Y_j = \{-\}$ , where  $-$  is null output.
- $\delta : S \times X \rightarrow S$  is the *next state function*.
- $\lambda_i : S \times X \rightarrow Y_i$  is the *output function on port  $i$* .

# Concurrent multi-port machines

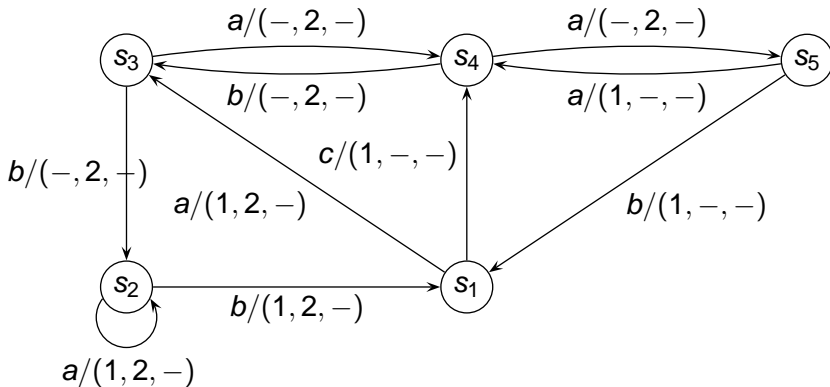


Figure: The multiports FSM  $M_0$



# Concurrent multi-port machines

In  $M_0$

- $S = \{s_1, s_2, s_3, s_4, s_5\}$
- $X_1 = \{a\}, X_2 = \{b\}, X_3 = \{c\}$
- $Y_1 = \{1\}, Y_2 = \{2\}, Y_3 = \{3\}$

# Concurrent multi-port machines

## Limitations with multi-port machines

One problem with p-multiport I/O Automata is that despite the fact that they are meant to specify distributed systems, they do it in a sequential way, one input at the time. This leads to a model that is

- **Inefficient** : every possible combination of concurrent inputs must be specified in the model
- **Unclear** : the causal relationships between inputs and outputs is not explicitly described

# Concurrent multi-port machines

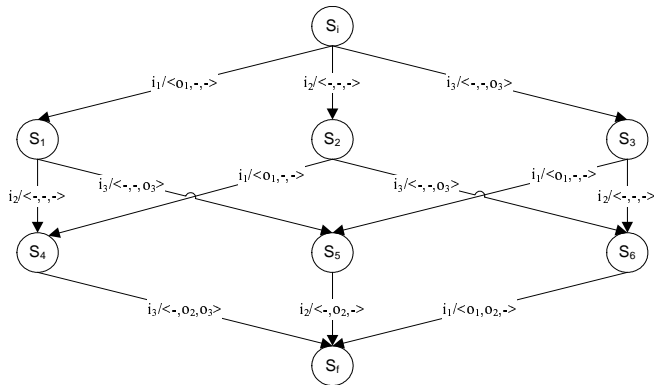


Figure: (Partial) Multiports Deterministic FSM.

# IO-PO-automata

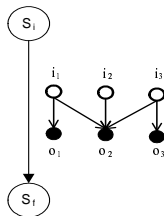
## A new model

We need a model that allows specifications to relax synchronization constraints: equipping partial order automata with input/output capabilities. We define a class of

**IO-PO-automata (IOPOA)** in which

- inputs can arrive asynchronously, and
- transitions may occur partially, and in several steps, reacting to inputs as they arrive and producing outputs as soon as they are ready, without dedicated synchronization.

# IO-PO-automata



**Figure:** The IOPOA corresponding to the multiports deterministic FSM  $M_0$ .

# IO-PO-automata

## Definition

An *Input/Output Partial Order Automaton* is a tuple

$\mathcal{M} = (S, \mathbf{s}^{\text{in}}, \text{Chn}, \mathcal{I}, \mathcal{O}, \delta, \lambda, \omega)$ , where

- $S$  is a finite set of *states* and  $s_1 = \mathbf{s}^{\text{in}} \in S$  is the *initial state*;
- $\text{Chn} = \pi_1, \dots, \pi_p$  is the set of *I/O channels (ports)*,
- $\mathcal{I}$  is the common *input alphabet*, and  $\mathcal{O}$  the common *output alphabet* for all channels.
- $\delta : S \times \mathcal{X} \rightarrow S$  is a (partial) next state function
- $\lambda : S \times \mathcal{X} \rightarrow \mathcal{Y}$  is the output function
- ...

# IO-PO-automata

## Definition

An *Input/Output Partial Order Automaton* is a tuple

$\mathcal{M} = (S, \mathbf{s}^{\text{in}}, \text{Chn}, \mathcal{I}, \mathcal{O}, \delta, \lambda, \omega)$ , where

- ...
- $\omega$  is a **PO transition label function**: For any  $(s, \mathbf{x}) \in S \times \mathcal{X}$  such that  $\delta(s, \mathbf{x}) = s'$  and  $\lambda(s, \mathbf{x}) = \mathbf{y} \in \mathcal{Y}$ ,  $\omega(s, \mathbf{x}) \subseteq (\{\mathbf{x}_1, \dots, \mathbf{x}_p\} \times \{\mathbf{y}_1, \dots, \mathbf{y}_p\})$  is a partial order that satisfies
  - $\mathbf{x}_i < \mathbf{y}_i$  for all  $i \in \{1, \dots, p\}$  such that  $\mathbf{x}_i \neq \perp$  and  $\mathbf{y}_i \neq \perp$ , and
  - if  $\mathbf{x}_i = \perp$ , then  $\mathbf{x}_i \not\leq \mathbf{y}_j$  for all  $j \in \text{Chn}$ .

# IO-PO-automata

## Strengths of the model

IOPOA do provide, as a model, a great improvement over p-multiport IO Automata in terms of

- **Size**: a single transition (a single order) can express a large number of transitions in the multiport model
- **Clarity**: causal relationships between input and outputs are explicitly described and do not have to be “guessed” by the implementer

## But...

What about testing? Are we “paying back” the efficiency of the model when generating test cases, with test sequences that are (exponentially) longer than the ones produced with multiport I/O



# IOPOA Distinguishing Sequence

## Definition (Distinguishing Sequence)

An IOPOA  $\mathcal{M}$  admits an **adaptive distinguishing sequence** if there is a set of  $n$  input sequences  $\{\xi_1, \dots, \xi_n\}$ , one per state of  $S$ , such that for all  $i, j \in [1, \dots, n], i \neq j$ ,  $\xi_i$  and  $\xi_j$  have a non-empty common prefix  $\xi_{ij}$  and  $\lambda(s_i, \xi_{ij}) \neq \lambda(s_j, \xi_{ij})$  or  $\omega(s_i, \xi_{ij}) \neq \omega(s_j, \xi_{ij})$ .

# IOPOA Checking Sequence

## Definition (Checking Sequence)

Let  $\mathcal{M}_1 = (S_1, \mathbf{s}_1^{\text{in}}, Chn, \mathcal{I}, \mathcal{O}, \delta_1, \lambda_1, \omega_1)$  be an IOPOA. A **checking sequence** of  $\mathcal{M}_1$  is an input sequence  $I$  which distinguishes  $\mathcal{M}_1$  from any IOPOA

$\mathcal{M}_2 = (S_2, \mathbf{s}_2^{\text{in}}, \mathcal{I}, \mathcal{O}, Chn, \delta_2, \lambda_2, \omega_2)$  in  $C(\mathcal{M}_1)$  that does not conform to  $\mathcal{M}_1$ , i.e. such that  $\forall \mathbf{s} \in S_2, \overline{\lambda_1}(\mathbf{s}_1^{\text{in}}, I) \neq \overline{\lambda_2}(\mathbf{s}, I)$  or  $\overline{\omega_1}(\mathbf{s}_1^{\text{in}}, I) \neq \overline{\omega_2}(\mathbf{s}, I)$ .

# Sequential Input Automata Testing

## States verification

Assuming that the machine starts in its initial state  $\mathbf{s}^{\text{in}} = \mathbf{s}_1$ , the following test sequence checks that the implementation has  $n$  states, each of which reacts correctly when input the distinguishing sequence for that state:

$$\xi_1 \circ \tau(\delta(\mathbf{s}_1, \xi_1), \mathbf{s}_2) \circ \xi_2 \circ \tau(\delta(\mathbf{s}_2, \xi_2), \mathbf{s}_3) \circ \dots \circ \xi_n \circ \tau(\delta(\mathbf{s}_n, \xi_n), \mathbf{s}_1) \circ \xi_1$$

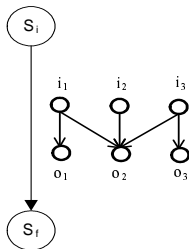
## Transitions verification

Testing a transition  $a/b$  going from  $\mathbf{s}_i$  to  $\mathbf{s}_j$ , assuming the implementation is in a state  $\mathbf{s}_k$ :

$$\tau(\mathbf{s}_k, \mathbf{s}_{i-1}) \circ \xi_{i-1} \circ \tau(\delta(\mathbf{s}_{i-1}, \xi_{i-1}), \mathbf{s}_i) \circ a \circ \xi_j$$

# Testing IOPOA

The “classical” approach to testing automata does not work with IPPOA because the causal relationships are not observed.

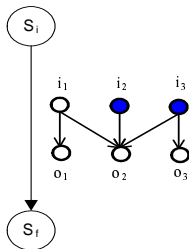


## Solution

- Delay input on one port
- Observe outputs
- Send last input
- Observe outputs
- repeat

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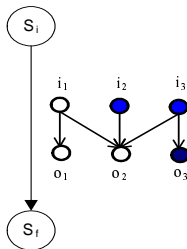


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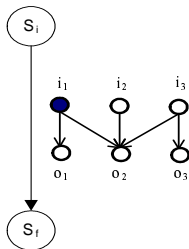


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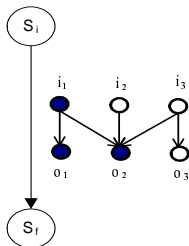


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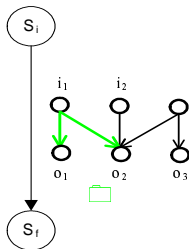
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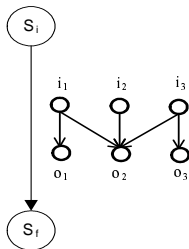


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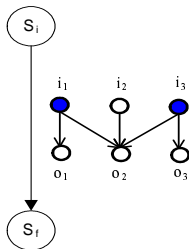


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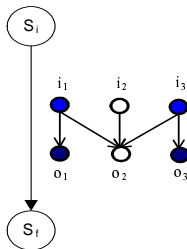


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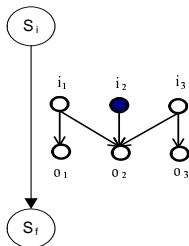


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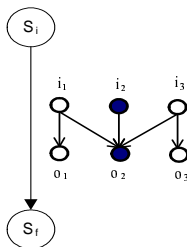


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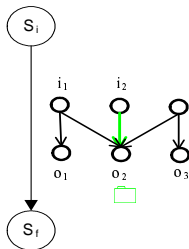


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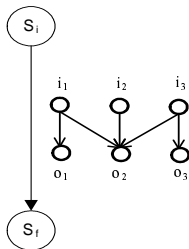


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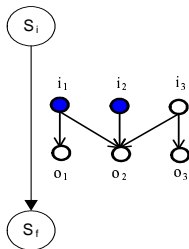
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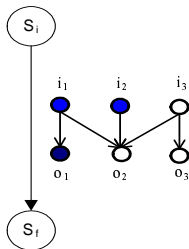


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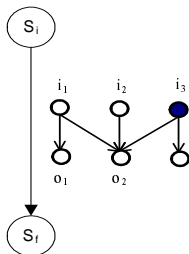


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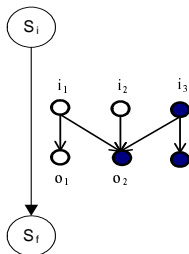


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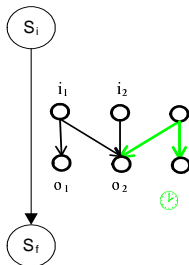


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# Testing IOPOA

## Delayed input testing

We define input vector  $\check{\mathbf{x}}^i$  as

$$\check{\mathbf{x}}_j^i \triangleq \begin{cases} \perp & : i = j \\ \mathbf{x}_j & : i \neq j, \end{cases}$$

$$\hat{\mathbf{x}}_j^i \triangleq \begin{cases} \mathbf{x}_i & : i = j \\ \perp & : i \neq j. \end{cases}$$

On a sequence  $\alpha = \alpha_1 \dots \alpha_n$

$$\Delta_i(\alpha) \triangleq \check{\alpha}_1^i \hat{\alpha}_1^i \check{\alpha}_2^i \hat{\alpha}_2^i \dots \check{\alpha}_n^i \hat{\alpha}_n^i$$

# State verification

## Theorem

*An implementation of an IOPOA, assumed to be in a state  $\mathbf{s}_k$  for which  $\xi_k$  is a distinguishing sequence, can be verified to have implemented  $\mathbf{s}_k$  with the following test sequence:*

$$\Gamma(\mathbf{s}_k) = \left[ \Delta_1(\xi_k) \circ \tau_{\mathbf{s}_k}^{\xi_k} \right]^n \circ \left[ \Delta_2(\xi_k) \circ \tau_{\mathbf{s}_k}^{\xi_k} \right]^n \circ \dots \circ \left[ \Delta_p(\xi_k) \circ \tau_{\mathbf{s}_k}^{\xi_k} \right]^n$$

*where  $[I]^n$  stands for the application of input sequence  $I$   $n$  times.*

# Checking Sequence construction

## Checking all states

$$\Gamma(\mathbf{s}_1) \circ \tau(\mathbf{s}_1, \mathbf{s}_2) \circ \Gamma(\mathbf{s}_2) \circ \tau(\mathbf{s}_2, \mathbf{s}_3) \circ \dots \circ \Gamma(\mathbf{s}_n) \circ \tau(\mathbf{s}_n, \mathbf{s}_1) \circ \Gamma(\mathbf{s}_1)$$

## Checking transitions

$$\Gamma(\mathbf{s}_i) \circ x \circ \Gamma(\mathbf{s}_j) \circ \tau_{\mathbf{s}_i}^x \circ \Gamma(\mathbf{s}_j) \circ \Delta_1(\mathbf{x}) \circ \tau_{\mathbf{s}_i}^x \circ \Delta_2(\mathbf{x}) \circ \tau_{\mathbf{s}_i}^x \circ \dots \circ \Delta_p(\mathbf{x}) \circ \tau_{\mathbf{s}_i}^x$$

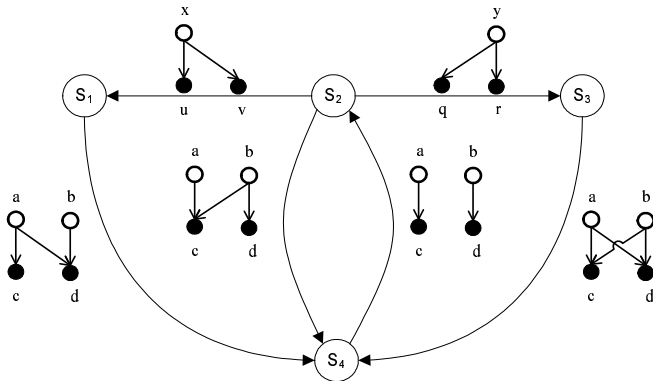


# Checking Sequence construction

## Theorem

*Given an IOPOA of  $n$  states and  $t$  transitions having an adaptive checking sequence, assuming that the implementation is in the initial state, the following test sequence is a checking sequence of size  $O(tpn^3 + pn^4)$*

# State identification and State Verification



**Figure:** An IOPOA for which states can neither be identified nor verified.

# Homing and Synchronizing sequences

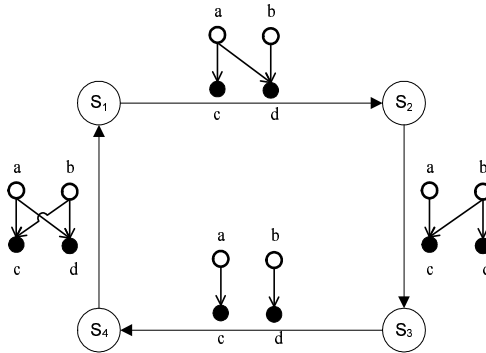


Figure: Homing sequences can be found for IOPOA.

## Further research directions

- Checking sequences for IOPOA without distinguishing sequences
- IOPOA with arbitrary partial order
- Petri Nets
- Sufficient conditions for weak synchronization at states
- On-going implementation