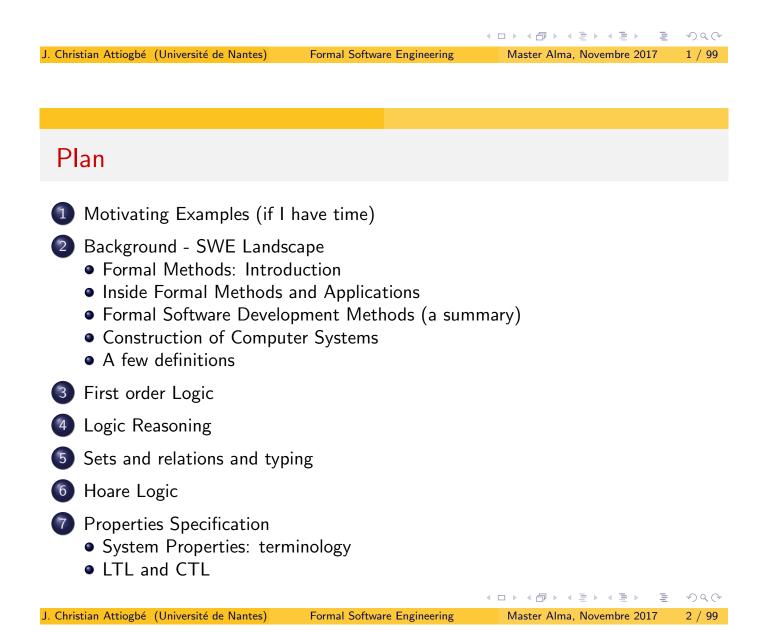
## Formal Software Engineering GL Formel

J. Christian Attiogbé

Master Alma, Novembre 2017



#### Dpt Info IUT

- Modélisation de données, Base de données,
- Algorithme et Programmation
- Algèbre linéaire
- Modélisation et programmation de systèmes répartis

**Dpt Info UFR Sciences** 

• Formal Software Engineering (Construction formelle de logiciels)

LS2N- UMR 6004 / Université de Nantes - CNRS - ECN - IMTA

J.	Christian	Attiogbé	(Université	de	Nantes
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Formal Software Engineering

AeLoS Team LS2N



	Tutel	les et Parten	aire :	
UN	CENTRALE NANTES	IMT Atlantique Britagne Phys de la Loire Ecole Mines-Jalecon	CITS	

#### Figure: Pôles de recherche du LS2N

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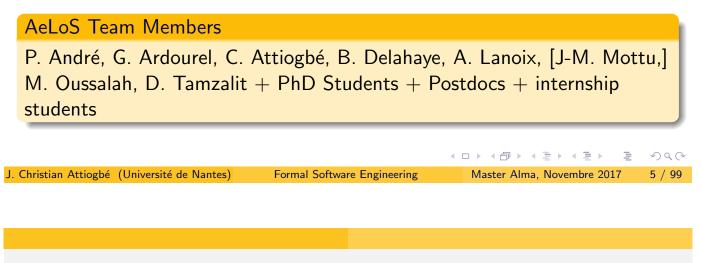
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#### AeLoS Team - LS2N

#### **Research Topics**

- Construction of Correct Architecture and Software
- Modelling, Verification, Refinement, Semantics
- Distributed Systems (services, components, architectures, properties)

Contact the team members for various internship projects, PhD projects, ...



## Presentation of this Course (24h)

Formal modelling and verification of software

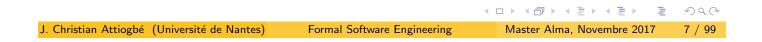
(the only way amenable to prove software correctness)

- Part 1 by Christian Attiogbé (~ 12 hours) Correct Construction with B Method, Event-B Atelier B/Rodin (theorem-proving).
- Part 2 by Claude Jard (~ 12 hours) Concurrency and Semantic Models ; Petri Nets/Romeo (model-checking), Timed Models/Uppaal (model-checking).

## Presentation of this Course (24h)

#### **Forecast Agenda**

Dates	Part 1	Part 2
	C. Attiogbé	C. Jard
08/11	Introductio	n FSE (CA)
09/11	CA	
15/11	CA	
22/11		Claude Jard
29/11		CJ
06/12		CJ



## About you - Motivations for this course

MASTER level  $\Rightarrow$  Managing industrial projects (computer systems) in various domains,

with variable size (small  $\cdots$  big)

Complex CS projects  $\Rightarrow$  Methods, Techniques, Tools

- Analysis Methods,
- Design & Verification Methods,
- Development/Implementation Methods.

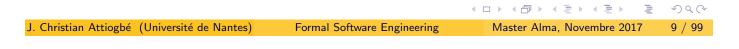
You probably already know some programming languages, semi-formal methods, [FM?]

Are you confortable with large CS projects, difficult problems, (what about the future)... ?

## 12h! - Rythm



Figure: Drumatic! (big-drum-purdue)



Motivating Examples (if I have time)

## Example: Web services interoperability (WS-AT)

Interoperability of services in distributed applications.

In distributed applications several services cooperate to achieve common goals. Pbm: How to build such interoperable, distributed applications with coordinated joint works? in an asynchronous context.

Web services tie together a large number of participants (they are services) forming large distributed computational units called activities. These activities are complex due to many parameters: interaction between participants, they can take long time...

To face the complexity, a framework to coordinate the activities is needed (it is the objective of WSCOOR, oasis). It enables participants to reach a consistent agreement on the outcome of distributed activities.

Several protocols have been proposed as basis for the interaction between Web services.

For example WS-Atomic Transaction (WS AT) contains protocols which are mechanisms to create activities, join into them, and reach common agreement on the outcome of joint operations.

## Example: Web services interoperability (WS-AT)

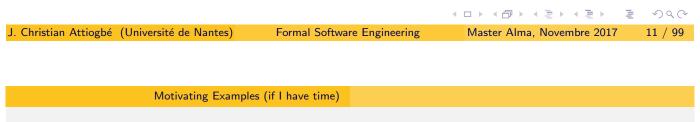
Def: An activity is a set of actions spaning multiple services but with a common goal (classical ex: resa).

The activities that require the ACID (atomic, consistent, isolated, and durable) properties of transactions are users of WS-Atomic Transaction.

An initiator creates/initiates an activity, and communicates its context to other applications. The other applications can register to participate in the activity. A coordinator manages all the participants of an activity. The coordinator at some point can decide to abort or to try to commit the transaction. Therefore it initiates (preparation phase) a vote to which all the participants participate. When there is a common positive agreement, it can commit the outcome (commit phase) of the trasaction (all or nothing).

Required Safety Property: to guarantee that the initiator and the participants agree on whether the transaction is committed or aborted.

http://docs.oas is - open.org/ws-tx/wstx-wsat-1.1-spec-os/wstx-wsat-1.1-spec-os.html



#### Example 1: a formal specification

```
MACHINE /* Sorting: a set of naturals -> seq. of natural */
Tri
CONSTANTS
tride /* defining a function */
PROPERTIES
tride : FIN(NAT) ---> seq(NAT) &
  (ran(tride(ss)) = ss &
    %(ii,jj).(ii : dom(tride(ss)) & jj : dom(tride(ss)) &
    ii < jj =>
        (tride(ss))(ii) < (tride(ss))(jj) ) ))
END</pre>
```

Emphasize abstraction = what (not how)

#### Example 2: a formal specification

```
system ProdCons /* Model */
sets
    DATA ;
    STATE = {empty, full}
variables
    buffer, bufferstate, bufferc
invariant
    bufferstate ∈ STATE
    ^ buffer ∈ DATA ∧ bufferc ∈ DATA
initialization
    bufferstate := empty
|| buffer :∈ DATA
|| bufferc :∈ DATA
end
```

Emphasize abstraction

```
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```

Motivating Examples (if I have time)

## Example 2: (continued)

ProdCons (continued)...

```
events

produce \widehat{=} / * when buffer empty * /

any dd where

dd \in DATA \land bufferstate = empty

then

buffer := dd ||

bufferstate := full

end ;

consume \widehat{=} / * when buffer is full * /

select bufferstate = full

then

bufferc := buffer ||

bufferstate := empty

end

end
```

Emphasize abstraction = what (not how)

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#### Examples of properties

Always an unique process in CS	card(activeProc) = 1
A process cannot be simultane- ously active and blocked	$activeProc \cap clockedProc = \emptyset$

The use of invariant properties

- Safety properties: nothing bad should happen
- Liveness properties: something good eventually happens More generally, one uses Modal Logics.



Background - SWE Landscape

## Categories/Natures of Software Systems

Nature of software systems	what Features?	which Methods?
sequential		
autonomous (transformational)		
centralised		
reactive		
real-time		
parallel		
parallel and concurrent		
distributed		
embedded		
communication protocols		

 $\Rightarrow$  various types of software systems, various methods

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## Semi-Formal Methods

#### Examples of semi-formal methods

- Functional Analysis (SA..., SADT),
- Structured Analysis (SA, SSADM), SA-RT,
- Entity-Relationship (Entités/Associations): Merise, Axiale,
- JSD/JSP,
- Object-Oriented Analysis, OMT, UML, Objectory Process (Ericsson, 1987), rational unified process (RUP),
- Software Architecture (System Level ; Top-Down approach),
- etc

#### Pros and Cons



#### Need of rigorous methods for some specific domains:

- Security, Certification, Cost, Maintenance
- ITSEC (Information Technology Security Evaluation Criteria) requires the use of **formal methods**
- Failure of (one flight) of ARIANE!, failure of a Pentium series, etc
- Environments which are dangerous for humans (nuclear, chemistry, marine, etc)
- Embedded Systems (vehicles, home equipments, etc)
- Automata (medical domain, etc)
- etc

#### Pros and cons

## Industry [already] adopts FM!

Difficulties for industries: Market Pressure, High costs, ··· BUT, there are numerous success stories

- Proof of a C compiler (Coq, Xavier Leroy, 2011) !!!
- Design of a Real-Time Operating System (TLA+)
   E. Verhulst, R.T. Boute, J.M. Sampaio Faria, B.H.C Sputh, V. Mezhuyev, Formal Development of a Network-Centric RTOS, 2011
- Airbus (Astrée, Scade/Simulink), Aerospace
- NASA (PVS, shuttle, ...), Boeing (...)
- Proof of IEEE 1395 Firewire Protocols (Spin, PVS, B, +++; 2004+)
- Proof of control systems (B, Siemens)
- Proof of circuit (STMicroelectronics)
- • •



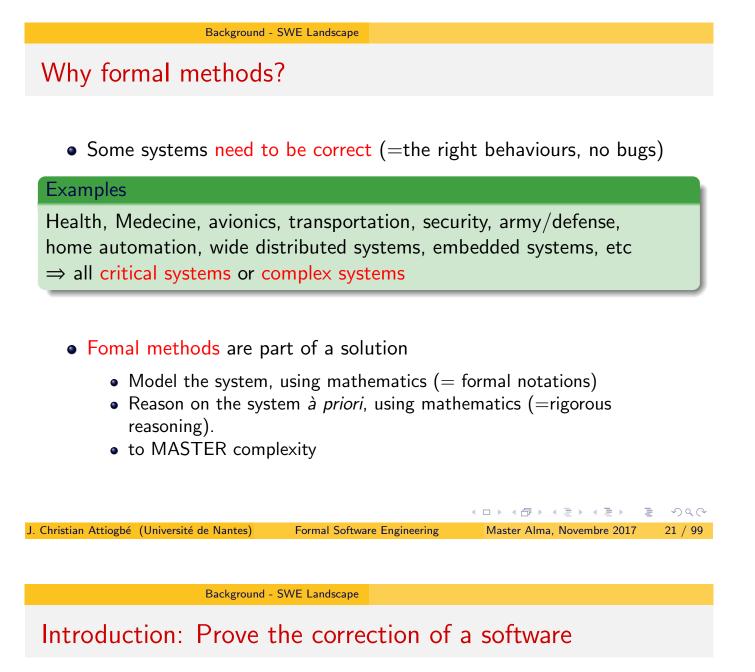
Industry [already] adopts FM!

- • •
- BOS barrier protecting the harbor of Rotterdam (Z, 2001)
- Proof of microcode and software (Intel)
- Proof of Communication Protocols (IO Automata, 1993+)
- • •

The complexity of current computer systems discourages empirical methods.

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#### Build correctly a software or Prove the correction of a software S via its model.

- The *model* of the software : *M*
- The properties : P
- $M \models P$

proof depending on the structure of the model ex: prove that P is true in all the (reachable) states of M(if M is a state model)

(if M is a state model) Anyway, you need a formal model; and/or rigorous software dev. methods. Do you know some?

Rearn how to build M, P and how to prove (Modelling + Verification) (using dedicated tools or not).

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#### What to learn?

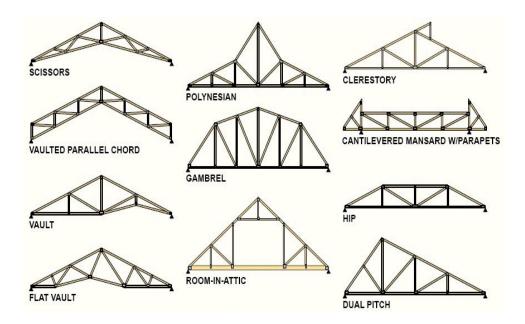
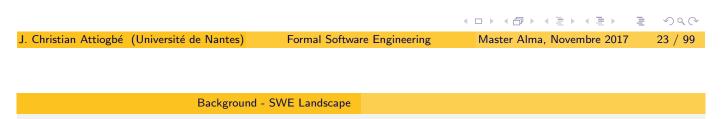


Figure: Truss styles (from caudilltrussandmetal.com)



#### Overview of formal methods and approaches

Deductive approaches (logic-based) Build a logic model of the system Prove the properties of a software/system, from the stated logical specifications = demonstrate a theorem from axioms; theorem proving Trends: Correct-by-construction (model, prove, refine until code)
State exploration approaches (automata-based) Build a state-based model of the system Check some properties in all the possible states of the software/systems model-checking; State-explosion; Symbolic model-checking; Statistic mdel-checking; ...
Static analysis (à posteriori, on the code/abstraction) with abstract

## Examples of models (you already know)

- Logics models (First Order, Higher Order, Modal)
- Axiomatic/algebraic models (equation systems)
- State-based models (Automata, LTS, graphs)
   Finite State Machines (Mealy, Moore, ...), Petri nets, Communicating processes,...
  - + various aspects: time, data, signals, probabilities
- Various classes of models and systems
  - Data-intensive models
  - Synchronous models Asynchronous models
  - Timed Systems Probabilistic (extension of Tansition systems)
  - Reactive systems, Embedded systems
  - ...



Background - SWE Landscape Formal Methods: Introduction

#### Features of Formal Methods

Formal methods  $\Rightarrow$  use rigorous approach to

- guaranty of software correction with respect to specifications,
- decrease/remove errors, and disfunctionning,
- make it easy the maintenance and the evolution.

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## Methods in Engineering

#### Construction methods of computer systems

A few analogies:

#### Building Engineering (Génie civil)

 $\rightarrow$  Architecture, schemes/blueprints (design), computings, construction (implementation)

#### Physics

 $\rightarrow$  Observations, modelling/study of models, implementation

#### Computer Science (Informatique)

Requirement Analysis (observations?)

Modelling - study of models,

Design and Implementation of systems.



#### Various approaches of formal methods:

- à postériori : First, one implements (programming paradigm) and then one verifies that the produced program is correct
  - $\rightarrow$  proof systems, testing, model-checking
- à priori : One builds correctly the system
  - $\rightarrow$  Development methods (refinement, synthesis), proof systems

Several formal methods (languages, proof systems, methods)

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#### Preliminaries

- Top-down approach: by decomposition
  - Global analysis (system study, system engineering)
  - Software Architecture
  - Implementation of components
    - Direct Programming or
    - Formal Development
- Bottom-up approach: composition of elementary components.
  - Study of available components,
  - Composition, reuse.

#### In all cases (approaches), make use of formal methods for

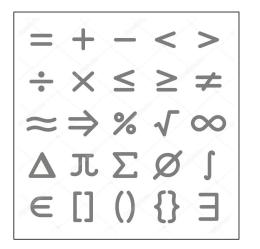
- Study of systems
- Study and construction of components/software
- Formal framework for reasoning, analysis, development.

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Background - SWE Landscape Inside Formal Methods and Applications

## What are inside formal methods?

- Logics
- Algebra
- Discrete Mathematics
- Set Theory
- Automata Theory
- Type Theory
- Refinement Theory
- ...



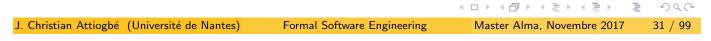
## Examples of a few industrial applications

#### with the B Method (J-R. Abrial)

GEC ALSTHOM, SNCF and MATRA Transport (now Siemens)

- Railway Speed Control System (KVS for SNCF)
- Line A of the Paris RER SACEM (signaling, speed control)
- Calcutta Metro (CTDC)
- Montreal Metro (CTDC), Marseille, Bel horizonte
- Météor (line 14, of Paris Metro, without human driver)
- Landing doors (portes pallières) in Metro stations
- Old people insurance, in French Sécurité Sociale
- CICS of IBM (major restructuring of a transactional, about 800000 lines of code)
- B and VDM are used in financial domain softwares, BULL UK

Many other systems with PVS, Coq, SPIN, Petri Nets, Lotos, etc



Background - SWE Landscape Inside Formal Methods and Applications

Example of the Railway Speed Control System (Metro)

- Data acquisition (sensors, converters, etc),
- Computation/decision,
- Orders sent to physical devices (speed slowing system, braking system),
- Embedding of the software in the global system of the train.

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#### Other used approaches, along the time

Some of them are equipped with tools and adopted by industries

LOTOS, SDL (european Standard) algebric approach + *communicating processes* Isabelle (Germany), PVS (USA) MEC/AltaRica (Université de Bordeaux + industries) Classical Logics: First order Logic, Hoare Logic, etc (Why, Frama-C, Krakatoa (Java), Key,...) Non-classical Logics, modal logics Coq, High-Order Logics, type theory



Interpretation of the Curry-Howard's Isomorphism:

Proof Axioms	equiv. to	Development	Specifications
Theorems	cquiv. to	Development	Programs

 $\rightarrow$  Proof assistants needed! not only editors and compilers

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## Overview of Software Construction

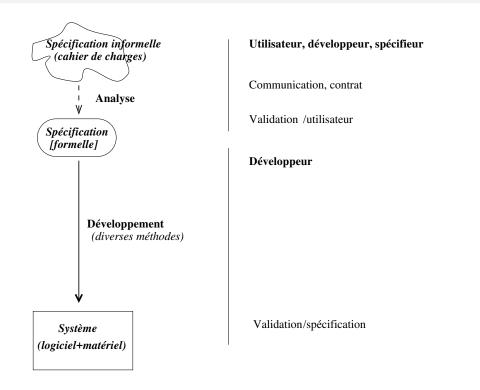
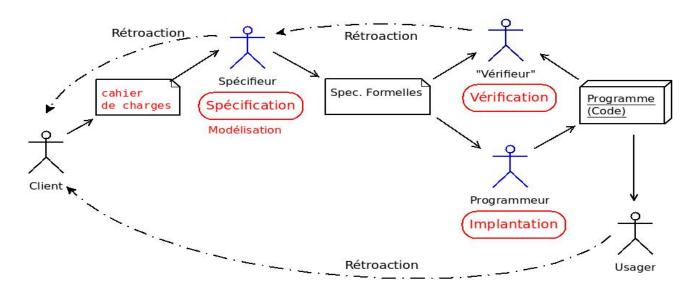


Figure: Issue of system development de system

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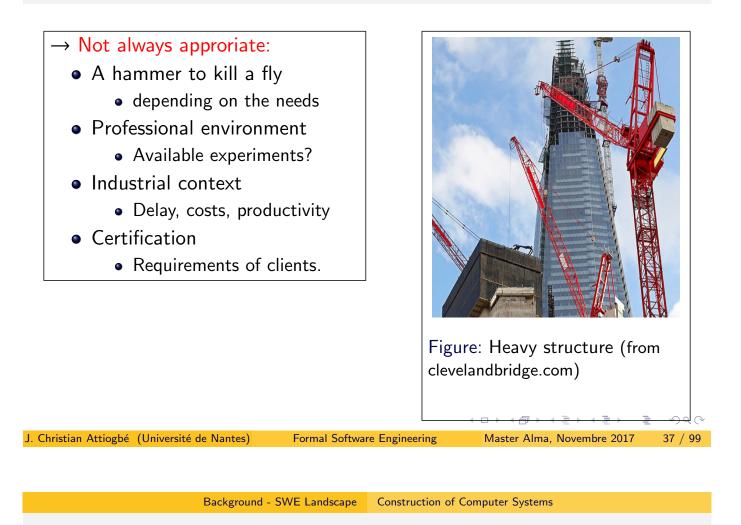
Background - SWE Landscape Construction of Computer Systems

## Overview of Software Construction



#### Figure: A life cycle of formal software construction

#### Use of Formal Methods



## Which approach to use?

#### $\rightarrow$ Several parameters:

- Designer/implementor of big systems,
- Designer/implementor of small (home) systems,
- Features of systems to be implemented,
- Available experiments,
- . . .

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## Categories/Natures of Software Systems

Nature of software/systems	what Features?	which Methods?
sequential		
autonomous (transformational)		
centralised		
reactive		
real-time		
parallel		
parallel and concurrent		
distributed		
embedded		
communication protocols		

 $\Rightarrow$  various types of software systems, various methods

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Background - SWE Landscape Construction of Computer Systems

#### A few difficult points

- To describe precisely the intended system specification
- To build correctly the sofware development
- To be sure that the constructed software is correct with respect to the needs
- Maintenance/Evolution of the system.

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## A few difficult points

- To describe precisely the intended system specification
- To build correctly the sofware development
- To be sure that the constructed software is correct with respect to the needs
- Maintenance/Evolution of the system.

Each project is unique

- Nature of complex systems → multifacets, modular
- Several methods, including:
  - Semi-formal methods
  - Formal Methods (integrated)  $\rightarrow$  to deal with complex systems.

#### $\Rightarrow$ mastering several methods

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	Background	- SWE Landscape	A few definitions			
A few de	efinitions					

#### Modelling:

Hoare: A scientific theory is formalised as a mathematical model of reality, from which can be deduced or calculated the observable properties and of a well-defined class of processes in the physical world.

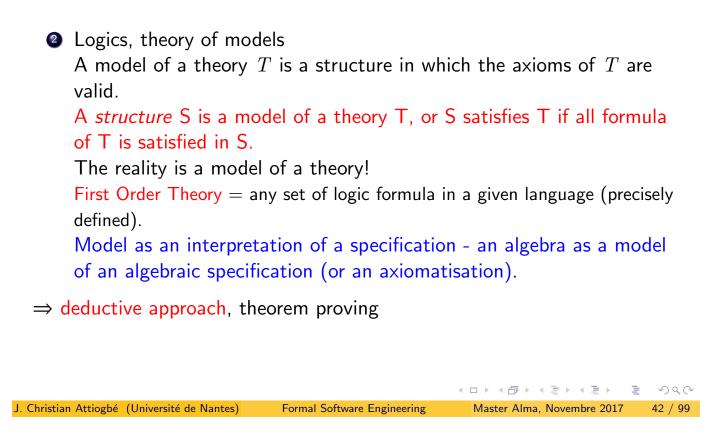
There are two main notions of models in computer science.

 Model = an approximation of the reality by a mathematical structure. An object O is a model of a reality R, if O allows one to answer all the questions about R.

In Mathematics, Physics, ... models are built with equation systems using quantities (masses, energy, ...) or hypothetic laws.

 $\Rightarrow$  State exploration, simulation

## A few definitions (continued)



 Background - SWE Landscape
 A few definitions

 A few definitions (continued)

These two notions of *model* are encountered in the model-oriented (or state-oriented) and property-oriented approaches of Soft. Eng. In current use,

- *model* = (archetype), what serves or is used for imitation to reproduce orther instances.
- *model* = (paradigm), declination model, conjugation model, etc
- *model* = (reference), . . .

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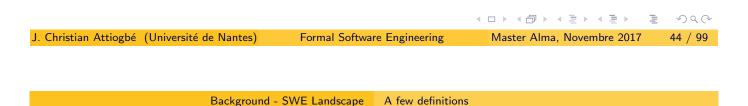
## A few definitions (continued)

#### Semiformal Method =

- Graphical Language [+ formal] (precise syntax and unprecise semantics) and
- Various analysis tools.

 $\rightarrow$  Combination of languages/methods/techniques that do not all have a precise semantics.

#### Examples : JSD, OMT, OOX, UML, Unified Process, RUP



## Interest and Limitations of Semi-formal Methods

- SADT, SA-RT, SSADM, ...
- JSD-JSP.
- Merise, Axial, ...
- OOA, OMT, UML, Unified Process, RUP
- . . .

The problem analysis is performed.

It is a positive contribution, although insufficient.

But, the problem is sided.

- $\rightarrow$  impossible to reason formally on the intended system.
- $\rightarrow$  there can be ambiguities and errors.

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## A few definitions (continued)

#### Formal Method =

- Formal Language (precise syntax and precise semantics) and
- Proof or formal reasoning system.

#### Examples: FSM, Petri, Z, CCS, CSP, HOL, Coq, PVS, B, ...

#### Formal Development =

• systematic transformation of specifications into programs using predefined laws/rules.

#### Synthesis, Refinement

Need Provers/assistants : Isabelle, Why, Coq, ...

#### Examples: B Method, Perfect, Escher C,...



**Verification:** to show that a system (S) is correct with respect to some properties (P)

 $S \models P$ 

**Validation:** to show that a system (S) is correct with respect to some informal properties (the needs)

 $S \sim S_{informal}$ 

Formal reasoning : Consists in applying a formal system to a specification.

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#### Examples of theory

Set theory: it is based on a set of axioms (Bourbaki, Cantor, Zermelo, ...). The objects of this theory are called sets.

The classe of the sets is called the universe.

The axioms of the set theory (of Zermelo+Fraenkel) are the following:



Background - SWE Landscape A few definitions

## Examples of theory (continued)

- Axiom of the empty set: there exists a set which does not contain any element: it is the empty set.
- Extensionality Axiom: two sets are equal if and only if they contain exactly the same elements.
- Union Axiom: the union of sets is a set.
- Axiom of the set of parts: given a set *E*, there exists a set *P* such a that a set *F* is member of *P* if *F* is a part of *E*.
- Axiom of replacing/substitution schema(Fraenkel, 1922) : When one defines a function with the formula of the set theory, the elements for which this function verifies a given property are also a set.

Moreover, to these axioms is added, the axiom of infinite: there exists an infinite ordinal.

ZFC = ZF + axiom of choice

• Axiom of choice: Given a family of disjoint sets, if we consider one element of each set of the family, then one builds another set.

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#### Some references

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- Success Stories www.fm4industry.org/index.php/DEPLOY\_Success\_Stories, www.fm4industry.org/index.php/Deploying\_Event-B\_in\_an\_ Industrial\_Microprocessor\_Development
- and Dijkstra, Hoare,...

Wing, Hehner, Monin, Hollow	vay, ···		~ ~ ~
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First order Logic

# Logics: Modelling and reasoning

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First order Logic

## Structure of the brain: logical part

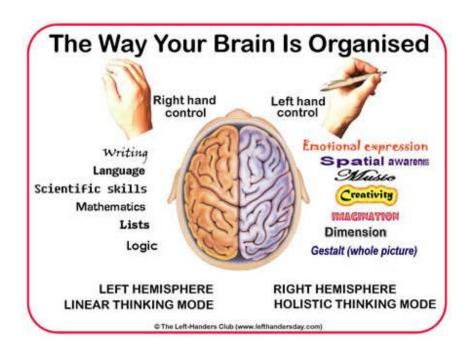


Figure: Brain organisation (from www.mindfulnet.org/page8.htm)

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	First order Logic		
First Order Logic			

A proposition is a sentence named P, Q, E... with a value TRUE or FALSE; the construction of a proposition is made with the following grammar:

 $\begin{array}{cccc} prop & ::= & P, Q, E, \dots \\ & | & prop \wedge prop \\ & | & \neg prop \\ & | & prop \Rightarrow prop \end{array}$ 

Parentheses can be used if necessary.

Other operators (logical connectors) :  $\lor$ , =

The semantics of a proposition (with the connectors) is given by a truth table (Exercice).

## Examples of Proposition

A cat with a hat is a Lion

Peter rides a bycicle

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		First and a Logic		
		First order Logic		
Predicat	es			

Propositional calculus deals with : absolute truth. Predicate calculus deals with : relative truth, it is an extension of propositional calculus.

$$x\in I\!\!N \Rightarrow x\geq 0$$

Two kinds of variables are used in predicates: free variables and bound variables which are introduced with quantifiers.

#### How to use predicates

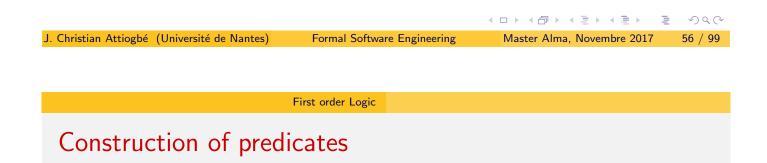
• Substitution

$$[x := 5](x \in \mathbb{N} \Rightarrow x \ge 0)$$
$$(5 \in \mathbb{N} \Rightarrow 5 \ge 0)$$
$$[x := elephant](BigEars(x) \Rightarrow African(x))$$

• Quantification

$$\forall x.BigEars(x) \Longrightarrow African(x),$$

 $\forall x. (Animal(x) \land BigEars(x)) \Longrightarrow African(x)$ 



#### First order Logic

## Usage of Logics

• for modelling : *predicates* 

predicate = formula to be proved

 $P \land Q$   $P \Rightarrow Q$  0 < 3  $\{0, 3\} \subset \{0, 4, 8, 3\}$ 

```
• for reasoning : sequents
```

$$H \vdash P$$

$$H : Hypotheses$$

$$P : conjecture$$

$$P : conjecture$$

Formal Software Engineering

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First order Logic

Inference rules of propositional calculus

∧ intr	$\frac{HYP \vdash P \qquad HYP \vdash Q}{HYP \vdash P \land Q}$	use backward to decom- pose into simple subgoals with the same hypothe- ses
$\land$ elim	$\frac{HYP \vdash P \land Q}{HYP \vdash P  HYP \vdash Q}$	
$\Rightarrow intr$	$\frac{HYP, P \vdash Q}{HYP \vdash P \Rightarrow Q}$	deduction rule
$\Rightarrow elim$	$\frac{HYP \vdash P \Rightarrow Q}{HYP, P \vdash Q}$	anti-deduction
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#### First order Logic

Modus Ponens	$\frac{HYP \vdash P}{HYP \vdash Q} \xrightarrow{HYP \vdash Q} Q$	
Contradiction	$\frac{HYP, \neg Q \vdash P \qquad HYP, \neg Q \vdash \neg P}{HYP \vdash Q}$	first rule for ¬
	$\frac{HYP, Q \vdash P \qquad HYP, Q \vdash \neg P}{HYP \vdash \neg Q}$	second rule for ¬

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Logic Reasoning

## Reasonning

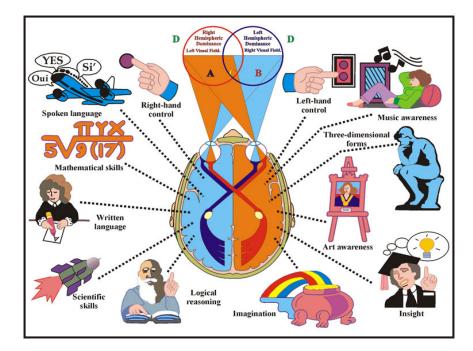


Figure: To mimic brain complexity (from ehealing.us)

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#### Reasoning

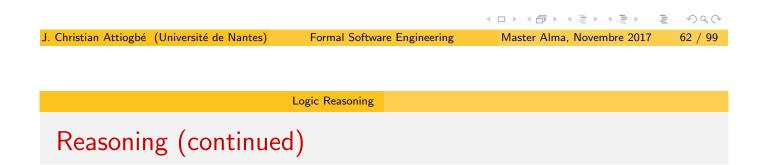
with a meta-language

#### • Inference rules

An inference rule links sequents and its defines a valid step of a proof. An inference rule has the following shape:

$$\frac{\sum_{1},\sum_{2},\ldots,\sum_{n}}{\sum}$$

The sequents  $\sum_1, \sum_2, \dots, \sum_n$  are called *antecedents*, and the sequent  $\sum$  is called *consequent*.



• Proof principle

To prove a sequent, one uses the inference rules

- as derivation rules : forward rule application,
- as reduction rules : backward rule application.

Implementation

• Theorem to prove / Inference To prove a theorem

 $P \vdash Q$ 

one transforms it into inference rule

$$\frac{H \vdash P}{H \vdash Q}$$

• Proofs : forward or backward - tactics

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# SETS: Modelling and reasoning

J. Christian Attiogbé (Université de Nantes)

Formal Software Engineering

Sets and relations and typing

## Structuring



Figure: Amazing steel structure (from clsteel)

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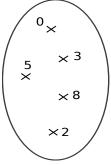
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## Sets and typing

 Predefined Sets (work as types) BOOL, CHAR, INTEGER (ℤ), NAT (ℕ), NAT1 (ℕ\*), STRING



• Cartesian Product  $E \times F$ 

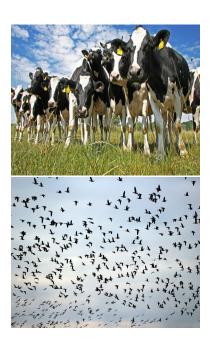


Figure: Sets of cows, birds

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	Sets and re	lations and typing		

Sets and typing

- The set of subsets (powerset) of E *P*(*E*) written POW(E)
- user defined abstract sets, enumerated sets



Figure: Set of sets of birds

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## Set Theory Language

#### The standard set operators

 ${\cal E}$  ,  ${\cal F}$  and  ${\cal T}$  are sets, x a member of  ${\cal F}$ 

Description	Notation	Ascii
union	$E \cup F$	E \/ F
intersection	$E \cap F$	E /\ F
membership	$x \in F$	x : F
difference	$E \setminus F$	E - F
inclusion	$E \subseteq F$	E <: F

+ generalised Union and intersection

+ quantified Union et intersection

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Sets and re	elations and typing		
Set Theory Language			

In ascii notation, the negation is written with /.

Description	Notation	Ascii
not member	$x \notin F$	x /: F
non inclusion	$E \not\subseteq F$	E /<: F
non equality	$E \neq F$	E /= F

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## Generalised Union (à la B)

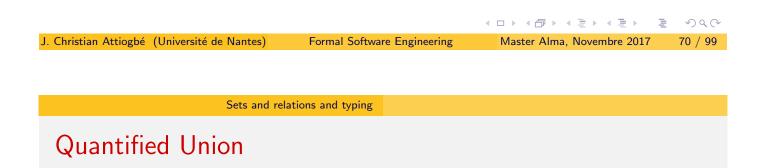
an operator to achieve the generalised union of well-formed *set expressions*.

$$S \in \mathcal{P}(\mathcal{P}(T))$$
  

$$\Rightarrow$$
  

$$union(S) = \{x \mid x \in T \land \exists u.(u \in S \land x \in u)\}$$
  
Example

$$union(\{\{aa, ee, ff\}, \{bb, cc, gg\}, \{dd, ee, uu, cc\}\})$$
  
=  $\{aa, ee, ff, bb, cc, gg, dd, uu\}$ 



an operator to achieve the quantified union of well-formed *set expressions*.

$$\forall x.(x \in S \implies E \subseteq T) \\ \Rightarrow \\ \bigcup x.(x \in S \mid E) = \{y \mid y \in T \land \exists x.(x \in S \land y \in E)\}$$
Exemple
Exemple

$$UNION(x).(x \in \{1, 2, 3\} \mid \{y \mid y \in NAT \land y = x * x\})$$
$$= \{1\} \cup \{4\} \cup \{9\} = \{1, 4, 9\}$$

# Generalised Intersection (à la B)

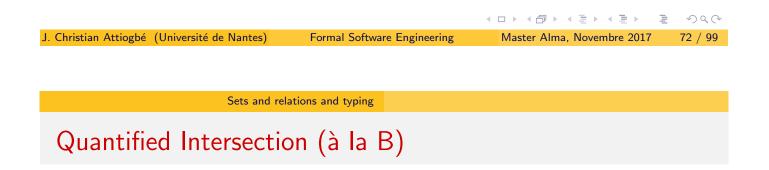
an operator to achieve the generalised intersection of of well-formed set expressions.

$$S \in \mathcal{P}(\mathcal{P}(T))$$
  

$$\Rightarrow$$
  

$$inter(S) = \{x \mid x \in T \land \forall u.(u \in S \Rightarrow x \in u)\}$$
  
Example  

$$inter(\{\{aa, ee, ff, cc\}, \{bb, cc, gg\}, \{dd, ee, uu, cc\}\} = \{cc\}$$



an operator to achieve the quantified intersection of of well-formed set expressions.

$$\forall x.(x \in S \implies E \subseteq T) \Rightarrow \cap x.(x \in S \mid E) = \{y \mid y \in T \land \forall x.(x \in S \implies y \in E)\}$$
  
Example  
$$INTER(x).(x \in \{1, 2, 3, 4\} \mid \{y \mid y \in \{1, 2, 3, 4, 5\} \land y > x\}) = inter(\{\{1, 2, 3, 4, 5\}, \{2, 3, 4, 5\}, \{3, 4, 5\}, \{4, 5\}\})$$

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# Relations

## RELATIONS

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Sets and relations and typing

# **Recurrence Relations**

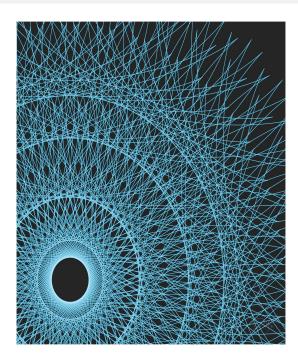


Figure: Amazing recurrence relation (from devanmatthews.files.wordpress.com)

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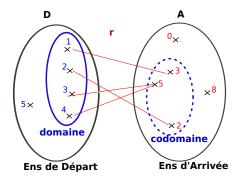
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# Relations: definition, vocabulary

A relation r over D and A is a subset of the cartesian product  $D \times A$ it is noted  $r: D \leftrightarrow A$  or  $r \subseteq D \times A$ r is a set of couples (d, a) also denoted by  $d \mapsto a$ 



 $r = \{(1, 3), (2, 2), (3, 5), (4, 5)\}$  ou  $r = \{1 \mapsto 3, 2 \mapsto 2, 3 \mapsto 5, 4 \mapsto 4\}$ 

dom $(r) = \{1, 2, 3, 4\}$ ran $(r) = \{3, 5, 2\}$ 

Figure: Euler-Venn diagram of r

Domaine : domaine	Codomaine : range		
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Sets and relations and typing			
Relations: definition	, vocabulary		

## S and T are sets.

An element of  $r: S \leftrightarrow T$  is a couple.

A element s of S can have several images in T.

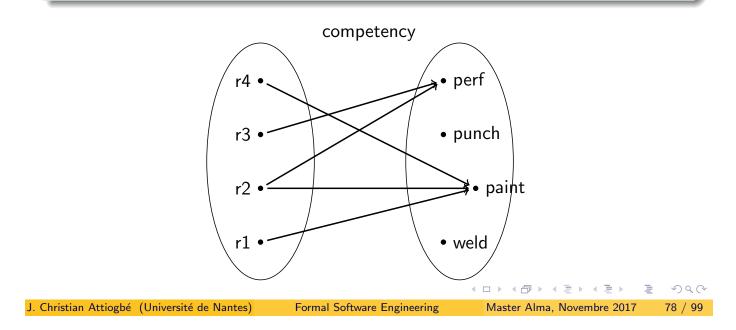
Description	Notation	Ascii
relation	$r : S \leftrightarrow T$	r : S <-> T
domain	$dom(r) \subseteq S$	dom(r) <: S
range	$ran(r) \subseteq T$	ran(r) <: T
composition	r;s	r;s
composition r(s)	$r \circ s$	r(s)
identity	id(S)	id(S)

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# Relations (continued)

#### Robots

Consider a plant with a set of polyvalent articulated robots, for welding, painting, punching, perforating, etc. Ho to model? know the available painting robots? and how many? ...

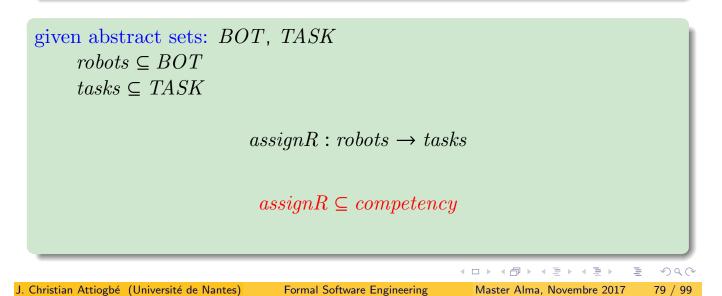


Sets and relations and typing

# Relations (continued)

#### Robots

Consider a plant with a set of polyvalent articulated robots, for welding, painting, punching, perforating, etc. A robot can be assigned at most only one task at time. But one task among its competencies



# Relations (continued)

## to build new relation r' from $r:S\leftrightarrow T$

Description	Notation	Ascii
domain restrictition	$S \triangleleft r$	S < r
range restriction	$r \triangleright T$	r  > T
domain antirestriction	$S \triangleleft r$	S <<  r
range antirestriction	$r \triangleright T$	r  >> T
inverse	$r^{\sim}$	r ~
relationnelle image	r[S]	r <mark>[S]</mark>
overiding	$r1 \oplus r2$	r1 <+ r2
direct product of rel.	$r1 \otimes r2$	r1 >< r2
closure	closure(r)	closure(r)
reflexive trans. closure	closure1(r)	closure1(r)

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Formal Software Engineering Mast

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Sets and relations and typing

Functions

## FUNCTIONS

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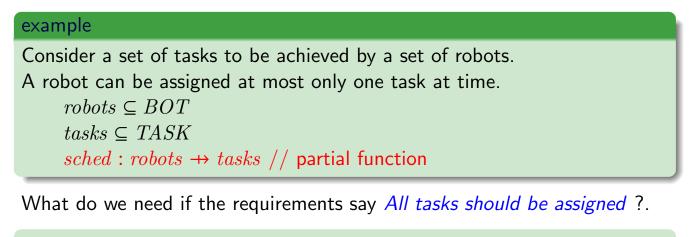
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# **Functions**

S and T are sets.  $f: S \rightarrow T$  a function

Unlike in a relation, an element of S can have at most one image via f.



sched : robots ++> tasks // partial sujective function

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Sets and relations and typing				
Function	S			

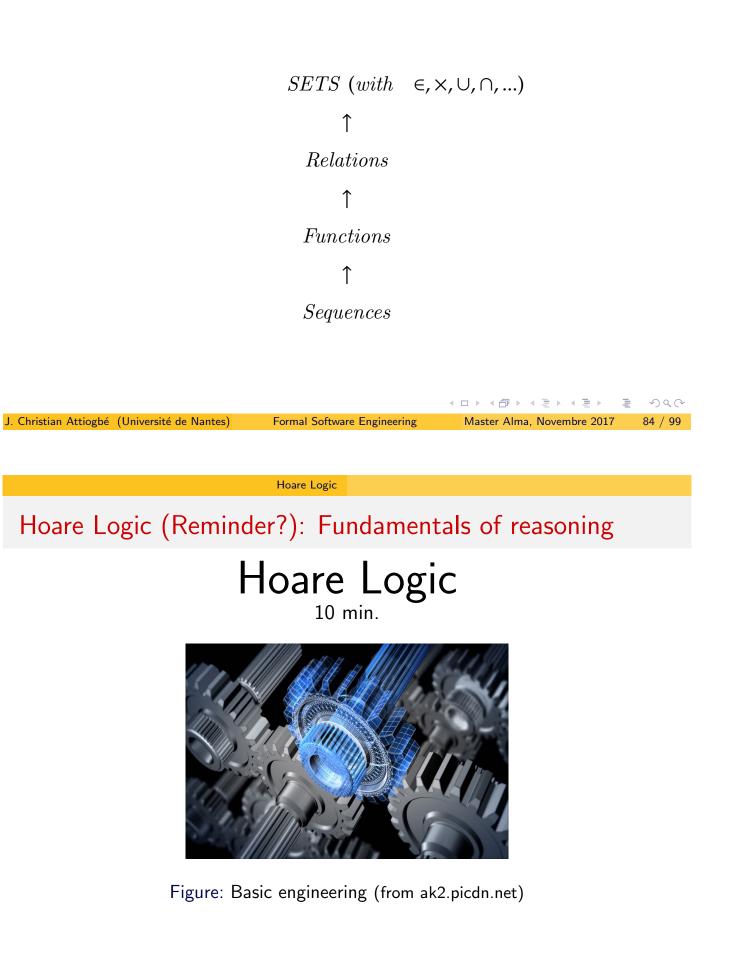
S and T are sets.  $f: S \rightarrow T$  a function

Unlike in a relation, an element of S can have at most one image via f in T.

Description	Notation	Ascii
partial function	$f: S \twoheadrightarrow T$	f : S +-> T
total function	$f: S \to T$	f : S> T
partial injection	$f: S \rightarrowtail T$	f : S >+-> T
total injection	$f: S \rightarrowtail T$	f : S >-> T
partial surjection	$f: S \twoheadrightarrow T$	f : S +->> T
total surjection	$f: S \twoheadrightarrow T$	f : S>> T
total bijection	$f: S \rightarrowtail T$	f : S >-> T
lambda abstraction	$\%x.(P \mid E)$	

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# Powerful mathematical structures



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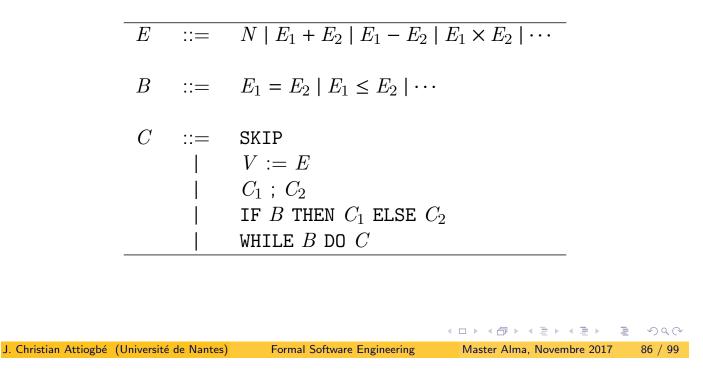
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#### Hoare Logic

# Floyd-Hoare Logic

Elementary to reason on the correction of programs Consider a pseudo-programming language, described by the grammar



	Hoare Logic
Floyd-Hoare Logic	

The Hoare triple denotes the partial correction of a statement.

P a formula of the first order logic,

 $\vdash P$  means P can be deducted from the laws of logics and arithmetics.

## $\vdash$ {P} C {Q} means that {P} C {Q} is

- either an instance of the schema of the axioms A1, A2 (above)
- or is deductible by a sequence of applications of the rules  $R_i$ .

#### Hoare Logic

Axioms and rules of Hoare logic

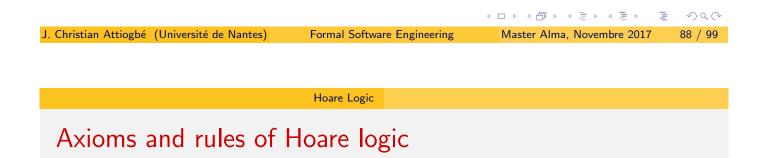
A1: Axiom of SKIP. For any formula P

$$\vdash \{P\}$$
 SKIP  $\{P\}$ 

A2: Substitution Axiom. P a formula, V a programme variable, E nd expression

$$\vdash \{P[E/V]\} \quad V := E \quad \{P\}$$

(P[E/V] denotes the result of the substitution of E to the free occurrences of V in P.)



R1: rule of the precondition (strengthening - renforcement)

$$\frac{\vdash P' \Rightarrow P \quad \vdash \{P\} \ C \ \{Q\}}{\vdash \{P'\} \ C \ \{Q\}}$$

R2: rule of the postcondition (weakening - affaiblissement)

$$\frac{\vdash \{P\} \ C \ \{Q\} \qquad \vdash Q \Rightarrow Q'}{\vdash \{P\} \ C \ \{Q'\}}$$

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#### Hoare Logic

# Axioms and rules of Hoare logic

R3: rule of the sequence

$$\frac{\vdash \{P\} \ C_1 \ \{Q\} \ \vdash \{Q\} \ C_2 \ \{R\}}{\vdash \{P\} \ C_1 ; C_2 \ \{R\}}$$

R4: rule of the IF structure

$$\begin{array}{c|c} \vdash \{P \land B\} & C_1 & \{Q\} & \vdash \{P \land \neg B\} & C_2 & \{Q\} \\ \hline \vdash \{P\} & \text{IF } B & \text{THEN } & C_1 & \text{ELSE } & C_2 & \{Q\} \end{array}$$

R5: rule of the WHILE structure

$$\vdash \{P \land B\} C_1 \{Q\}$$
  
$$\vdash \{P\} \text{ WHILE } B \text{ DO } C_1 \{Q \land \neg B\}$$

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Formal Software Engineering Master Alma, Novembre 2017

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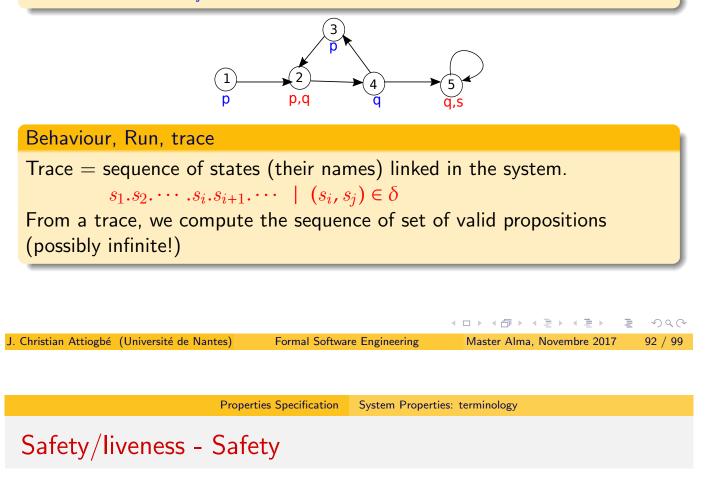
Properties Specification

# System Properties (6 min.)



### Kripke Structure (Saul Kripke, 1960)

Directed graph used as internal representation of software. Each state has a name/label and a list of propositions in  $\mathcal{P}$  which are valid in this state.  $(S, S_{init}, S_{final}, \delta : S \leftrightarrow S, \sigma : S \rightarrow \mathcal{P})$ 



#### Safety property

Safety property expresses that "something bad must not happen"

#### Examples:

- The index values never over the bounds.
- Only one vehicle will be in the tunnel (critical section)
- The program never loose the requests

Predicate Logic(+ set theory): logic for specifying liveness properties

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# Safety/liveness - Liveness

Liveness property

Liveness property expresses that "something good must happen" (in the future runs)

Examples:

- The user will get her access after the attempts of connection.
- All requests will be treated before the server closing

Temporal Logic: logic for specifying properties over time (Behavior of a finite-state system)



- The majority of properties are safety properties
- Liveness properties are often considered as more complicated safety properties (for instance with real-time response constraints)

Learn how to specify both; it depends on the project under work.

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# Linear-Time Logic (LTL) - Pnueli, during 1970

- Used to describe properties on individual execution traces (succession of dates)
- each moment in time has a well-defined successor moment. (function)
- Semantics: a set of (execution) traces

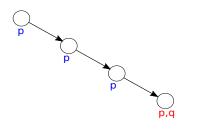




Figure: Pêche à la ligne (from madfred-angling.com)

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Properties Specification LTL and CTL

# Computation Tree Logic (CTL) - Branchng Time family

- Used to describe properties on several execution traces simultaneously (using quantifiers on the traces).
- from a state, reason about multiple possible time. (relations)
- Semantics: defined on terms of states

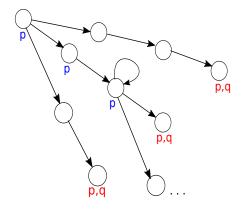


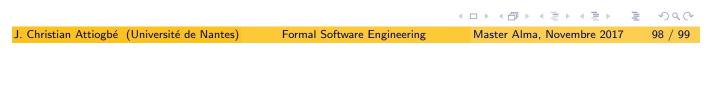


Figure: Pêche au filet (from esoxiste.com)

# Tools and References

Model checking: exponential in the size of LTL formula ; linear for TCL formula. For both LTL, CTL, model checking is linear in the size of the state graph.

Some model checking tools: SPIN, SMV, BLAST (Turing Award 2007: Clarke, Emerson, Siffakis) BLAST, CADP, UPPAAL, PRISM, CBMC UPPAAL-SMC, PLASMA, ...



#### Properties Specification LTL and CTL

## Tools and References

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